## Assignment 4

The ten questions below cover Units 11-13 and each carries equal weight. You are expected to solve all questions in detail and submit by uploading to the appropriate drop box. Scanned copy of your handwritten solutions should be acceptable.

1. A 4.00-kg particle moves in the $x y$ plane with a constant speed of $9.00 \mathrm{~m} / \mathrm{s}$ along the direction of the vector $(\hat{\imath}-\hat{\jmath})$. When the particle is at the position $(4.00 \mathrm{~m}, 0)$ calculate its the angular momentum relative to the point ( $2.00 \mathrm{~m}, 0$ ).
2. A $10.0-\mathrm{kg}$ disk, of radius 50.0 cm , rotates while experiencing variable torque given by the equation $\tau=(3.00 t-2.00) \mathrm{N} \cdot \mathrm{m}$. At $t=2.00 \mathrm{~s}$, the disk has angular momentum equal to $6.00 \mathrm{~kg} \cdot \mathrm{~m}^{2} / \mathrm{s}$. Calculate its angular speed and angular momentum at $t=5.00 \mathrm{~s}$
3. A small 60.0 g block slides down a frictionless surface through a height $h=25.0 \mathrm{~cm}$ and then sticks to the lower end of a vertical rod of mass 150 g and length 50.0 cm . The rod pivots about a point near its upper end through an angle $\theta$ before momentarily stopping. Find $\theta$.

4. A 32.0 kg child sits near the edge of a rotating merry-go-round that has the shape of a uniform disk of mass 60.0 kg and diameter 2.00 m . When the rotational speed is $\omega=1.00 \mathrm{rad} / \mathrm{s}$, the child catches a ball of mass 0.500 kg thrown by her mom. Just before the ball is caught, it has a horizontal velocity of magnitude $v=16.0 \mathrm{~m} / \mathrm{s}$ at an angle $\theta=30.0^{\circ}$ with a line tangent to the outer edge of the merry-go-round, as shown. Calculate the angular speed of the merry-goround just after the ball is caught.

5. A horizontal beam of length 9.0 m and mass 30 kg is hinged at the wall, with the far end supported by a cable that makes an angle of $60^{\circ}$ with the horizontal. A 20 kg sign hangs from the beam by two cables as shown. The cable can sustain a maximum tension of 900 N . A 76 kg man starts at the hinge and walks on the beam towards the sign. Calculate:
a. the maximum distance the man can walk safely
b. the reaction forces at the hinge just before the cable breaks

6. Two ladders, 4.0 m and 3.0 m long, are hinged at point A and tied together by a horizontal rope 75 cm above a frictionless surface, as shown. The mass of the longer ladder is 30 kg and that of the shorter one is 20 kg .
a. Calculate the upward reaction forces at the bottom of each ladder.
b. Calculate the tension in the rope.

7. A square ceramic tile of side width 50 cm is prepared to fit around an edge. A square section of side length 25 cm is cut from one corner of the tile, as shown. As a result, the centre-ofmass of the tile shifts from point A to point B. Find the distance between the two points.

8. A satellite moves in a circular orbit of radius $5.20 \times 10^{4} \mathrm{~km}$ around a planet with a period of 62.0 hours. If the gravitational acceleration near its surface is $6.80 \mathrm{~m} / \mathrm{s}^{2}$, calculate the planet's mass and radius.
9. A particle of mass $m$ is placed at a point along the axis of a ring at a distance $d$ from its centre, as shown. The ring has a mass $M$ and radius $a$.
a. Calculate the gravitational potential energy of the system.
b. Show that when $a \ll d$ the gravitational potential energy reduces to that between two point particles.

10. A weightlifter can lift 120 kg on Earth. What mass could the same person lift on
a. the moon?
b. the sun?
(See Table 13.2 in the textbook for planetary data.)
